

# Implicit Differentiation

## Implicit versus Explicit

Explicit: \_\_\_\_\_

Implicit: \_\_\_\_\_

Determine whether each function is defined implicitly or explicitly:

1.  $y = 5x^3 - 2x^2 + 3x - 2$

2.  $8x^2 + 3xy + 4y^2 = 1$

**Examples:** Find  $\frac{dy}{dx}$ .

1.  $y = 5x^3 - 2x^2 + 3x - 2$

2.  $8x^2 + 3xy + 4y^2 = 1$

**More Examples:** Find  $\frac{dy}{dx}$  and the slope of the tangent line at the given point.

3.  $x^2 + y^2 = 1$ ,  $(0, 1)$

4.  $4x^2 - 2y^2 = 9$ ,  $(3/2, 0)$

5.  $x^3 + y^3 = 3xy$ ,  $(3/2, 3/2)$

6.  $y^2 - x + 1 = 0$ ,  $(2, -1)$

## Implicit Differentiation

**Class Work:** Find  $\frac{dy}{dx}$  and the slope of the tangent line at the given point.

1.  $x^2 - y^2 = 16$ , (5, -3)

2.  $xy + y = 9$ , (2, 3)

3.  $x^2y + xy^2 = 2x$ , (1, 1)

4.  $(x + y)^2 + y = 2$ , (0, 1)

5.  $x^2 + 4y^2 = 4$ , (2, 0)

Extra Credit: 6.  $y + \sqrt{xy} = 4$ , (2, 2)